### Deep Probabilistic Programming (for Healthcare)\*

\*Thanks for Sriraam Natarajan (UT Dallas) and many others for all the great collaborations



Kristian Kersting









Getting deep systems that reason and know when they don't know Responsible Al systems that explain their decisions and co-evolve with the humans Open Al systems that are easy to realize and deal with complex data and knowledge

### AI has impact



Data are now ubiquitous; there is great value from understanding this data, building models and making predictions

However, there are not enough data scientists, statisticians, machine learning and AI experts.



### The third wave of Al



Data are now ubiquitous; there is great value from understanding this data, building models and making predictions

However, there are not enough data scientists, statisticians, machine learning and AI experts.



Al systems that can acquire human-like communication and reasoning capabilities, with the ability to recognise new situations and adapt to them.



### Potentially much more powerful than shallow architectures, represent computations

[LeCun, Bengio, Hinton Nature 521, 436-444, 2015]





#### **Differentiable Programming**

Markov Chain (MC)









### Potentially much more powerful than shallow architectures, represent computations

DePhenSe

Bundesanstalt für Landwirtschaft und Ernährung

[LeCun, Bengio, Hinton Nature 521, 436-444, 2015]

### They "develop intuition" about complicated biological processes and generate scientific data

[Schramowski, Brugger, Mahlein, Kersting 2019]

1.02k



### Potentially much more powerful than shallow architectures, represent computations

[LeCun, Bengio, Hinton Nature 521, 436-444, 2015]



SHARE REPORTS PSYCHOLOGY



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Science 14 Apr 2017: Vol. 356, Issue 6334, pp. 183-186 D0I: 10.1126/science.aal4230

### They "capture" stereotypes from human language



### Potentially much more powerful than shallow architectures, represent computations

[LeCun, Bengio, Hinton Nature 521, 436-444, 2015]

### **The Moral Choice Machine**





### **The Moral Choice Machine**

Dos	WEAT	Bias	Don'ts	WEAT	Bias
smile	0.116	0.348	rot	-0.099	-1.118
sightsee	0.090	0.281	negative	-0.101	-0.763
cheer	0.094	0.277	harm	-0.110	-0.730
celebrate	0.114	0.264	damage	-0.105	-0.664
picnic	0.093	0.260	slander	-0.108	-0.600
snuggle	0.108	0.238	slur	-0.109	-0.569

### But lucky they also "capture" our moral choices

[Jentzsch, Schramowski, Rothkopf, Kersting AIES 2019]



### Can we trust deep neural networks?



## DNNs do not quantify all of the uncertainty. They are not calibrated joint distributions. $P(Y|X) \neq P(Y,X)$

### MNIST



# SVHN

SEMEION

Train & Evaluate

**Transfer Testing** [Bradshaw et al. arXiv:1707.02476 2017]



[Peharz, Vergari, Molina, Stelzner, Trapp, Kersting, Ghahramani UDL@UAI 2018]

### Getting deep systems that know when they don't know.

### Sum-Product Networks: A deep probabilistic learning framework



... convex sum
 ... product
 ... distribution

completeness sum children: same scope

decomposability product children:

non-overlapping scope



Computational graph (kind of TensorFlow graphs) that encodes how to compute probabilities

### Inference is linear in size of network



### And there is a principled approach to select SPNs from data

Testing independence of random variables using e.g. (nonparametric) tests



[Poon, Domingos UAI'11; Molina, Natarajan, Kersting AAAI'17; Vergari, Peharz, Di Mauro, Molina, Kersting, Esposito AAAI '18; Molina, Vergari, Di Mauro, Esposito, Natarajan, Kersting AAAI '18]



SPFlow, an open-source Python library providing a simple interface to inference, learning and manipulation routines for deep and tractable probabilistic models called Sum-Product Networks (SPNs). The library allows one to quickly create SPNs both from data and through a domain specific language (DSL). It efficiently implements several probabilistic inference multiples like commuting matricels, coefficiently and (approximate) most explosed into (MDEs) along with commune.

### **Random sum-product networks**

[Peharz, Vergari, Molina, Stelzner, Trapp, Kersting, Ghahramani UDL@UAI 2018]

-200000 -150000 -100000 -50000

input log likelihood

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Cross-

(1.63M)

(0.22M)

(0.22M)



0



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### Learning the Structure of Autoregressive Deep Models such as PixelCNNs [van den Oord et al. NIPS 2016]



Learn Conditional SPN by testing conditional independence and using conditional clustering, using e.g. [Zhang et al. UAI 2011; Lee, Honovar UAI 2017; He et al. ICDM 2017; Zhang et al. AAAI 2018; Runge AISTATS 2018]

### **Conditional SPNs**

[Shao, Molina, Vergari, Peharz, Kersting 2019]







### Distribution-agnostic Deep Probabilistic Learning



Use nonparametric independency tests and piece-wise linear approximations





### Distribution-agnostic Deep Probabilistic Learning



However, we have to provide the statistical types and do not gain insights into the parametric forms of the variables. **Are they Gaussians? Gammas? ...** 

[Vergari, Molina, Peharz, Ghahramani, Kersting, Valera AAAI 2019]



Max Planck Institute for Intelligent Systems

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and Research

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### The Explorative Automatic Statistician

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CAMBRIDGE

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We can even automatically discovers the statistical types and parametric forms of the variables









### That is, the machine understands the data with few expert input ...



### ...and can compile data reports automatically

# P( heart | III )?



# P( heart | attack



)?





# P( heart attack



### Crossover of ML and DS with data & programming abstractions

De Raedt, Kersting, Natarajan, Poole: Statistical Relational Artificial Intelligence: Logic, Probability, and Computation. Morgan and Claypool Publishers, ISBN: 9781627058414, 2016.



#### Nat Rev Genet. 2012 May 2;13(6):395-405

### Heart diseases and strokes – cardiovascular disease – are expensive for the world

According to the World Heart Federation, cardiovascular disease cost the European Union EURO169 billion in 2003 and the USA about EURO310.23 billion in direct and indirect annual costs. By comparison, the estimated cost of all cancers is EURO146.19 billion and HIV infections, EURO22.24 billion



### Electronic Health Records A new opportunity for Al to save our Lifes









### **Statistical Relational Models**



#### Weighted logical formulas / uncertain databases





### Learning statistical models over databases: Functional Gradient Boosting

Learn multiple weak is easier than a single complex model



Friedman et al 2001, Dietterich et al. 2004, Natarajan et al. MLJ 2012



### **Functional Gradients for SRL Models**

Pseudo probability of an example

$$P(x_i = true | \mathbf{Pa}(x_i)) = \frac{e^{\psi(x_i; \mathbf{Pa}(x_i))}}{e^{\psi(x_i; \mathbf{Pa}(x_i))} + 1}$$

**Functional gradient** 

Maximize e.g. Pseudo Log Likelihood

$$LL(\mathbf{X} = \mathbf{x}) = \sum_{x_i \in \mathbf{x}} \log P(x_i | \mathbf{Pa}(x_i))$$

Gradient of pseudo log-likelihood w.r.t  $\psi$  for learning gradient models

$$\Delta(x_i) = \frac{\partial \log P(\mathbf{X} = \mathbf{x})}{\partial \psi(x_i; \mathbf{Pa}(x_i))} = I(x_i = true; \mathbf{Pa}(x_i)) - P(x_i = true; \mathbf{Pa}(x_i))$$

Sum all gradient models to get final  $\boldsymbol{\psi}$ 

$$\psi_m = \psi_0 + \Delta_1 + \ldots + \Delta_m$$

Extended to multiple SRL models & in presence of hidden data



X	Δ	
target(x1)	0.7	
target(x2)	-0.2	
target(x3)	-0.9	

Natarajan, Khot, Kersting, Shavlik. Boosted Statistical Relational Learners. Springer Brief 2015

Relational

### **Understanding Electronic Health Records**



[Kersting, Driessens ICML'08; Karwath, Kersting, Landwehr ICDM'08; Natarajan, Joshi, Tadepelli, Kersting, Shavlik. IJCAI'11; Natarajan, Kersting, Ip, Jacobs, Carr IAAI `13; Yang, Kersting, Terry, Carr, Natarajan AIME '15; Khot, Natarajan, Kersting, Shavlik ICDM'13, MLJ'12, MLJ'15, Yang, Kersting, Natarajan BIBM`17] Natarajan, Khot, Kersting, Shavlik. Boosted Statistical Relational Learners. Springer Brief 2015





### https://starling.utdallas.edu/software/boostsrl/wiki/

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#### BOOSTSRIL BASICS

Getting Started File Structure **Basic Parameters** Advanced Parameters Basic Modes Advanced Modes

#### ADVANCED BOOSTSRL

Default (RDN-Boost) MLN-Boost Regression One-Class Classification Cost-Senaltive SRL Learning with Advice Approximate Counting Discretization of Continuous-Valued Attributes. Lifted Relational Random Walks Grounded Relational Random Walks

**APPLICATIONS** 

Natural Language Processing

#### BoostSRL Wiki

THE UNIVERSITY **OF TEXAS AT DALLAS** 

BoostSRL (Boosting for Statistical Relational Learning) is a gradient-boosting based approach to learning different types of SRL models. As with the standard gradient-boosting approach, our approach turns the model learning problem to learning a sequence of regression models. The key difference to the standard approaches is that we learn relational regression models i.e., regression models that operate on relational data. We assume the data in a predicate logic format and the output are essentially first-order regression trees where the inner nodes contain conjunctions of logical predicates. For more details on the models and the algorithm, we refer to our book on this topic.

Sriraam Natarajan, Tushar Khot, Kristian Kersting and Jude Shavlik, Boosted Statistical Relational Learners: From Benchmarks to Data-Driven Medicine . SpringerBriefs in Computer Science, ISBN: 978-3-319-13643-1, 2015

### Human-in-the-loop learning

### New field: Deep Probabilistic Programming

In general, computing the exact posterior is intractable, i.e., inverting the generative process to determine the state of latent variables corresponding to an input is time-consuming and error-prone.

import pyro.distributions as dist

def model(data):
 # define the hyperparameters that control the beta prior
 alpha@ = torch.tensor(10.0)
 beta@ = torch.tensor(10.0)
 # sample f from the beta prior
 f = pyro.sample("latent\_fairness", dist.Beta(alpha@, beta@))
 # loop over the observed data
 for i in range(len(data)):
 # observe datapoint i using the bernoulli
 # likelihood Bernoulli(f)
 pyro.sample("obs\_{}".format(i), dist.Bernoulli(f), obs=data[i])

#### (2) Ease the implementation by some highlevel, probabilistic programming language



(1) Instead of optimizating variational parameters for every new data point, use a deep network to predict the posterior given X [Kingma, Welling 2013, Rezende et al. 2014]







[Stelzner, Molina, Peharz, Vergari, Trapp, Valera, Ghahramani, Kersting ProgProb 2018]

### **Sum-Product Probabilistic Programming**



(1) Instead of optimizating variational parameters for every new data point, use a deep network to predict the posterior given X [Kingma, Welling 2013, Rezende et al. 2014]

### **Sum-Product Attent-Infer Repeat**



A graphical model implemented in neural fashion using an VAE as object represention [Eslami, Heess, Weber, Tassa, Szepesvari, Kavukcuoglu, Hinton NIPS 2016]

### **Sum-Product Attent-Infer Repeat**



[Stelzner, Peharz, Kersting ICML 2019]





### There are strong invests into (deep) probabilistic programming

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RelationalAI, Apple, Microsoft and Uber are investing hundreds of millions of US dollars





relationalAI Al for the enterprise



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Intelligent Systems

Microsoft<sup>®</sup>



#### MORGAN &CLAYTOOL FUBL

Statistical Relational Artificial Intelligence Logic, Probability, and Computation

Luc De Raedt Kristian Kersting Seiraam Natarajar David Poole



Getting deep systems that reason and know when they don't know

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> Responsible Al systems that explain their decisions and co-evolve with the humans

Open Al systems that are easy to realize and understandable for the domain experts

"Tell the AI when it is right for the wrong reasons and it adapts its behavior"



(a) Original Image (b) Explaining Electric guitar (c) Explaining Acoustic guitar (c) Explaining Laborador Figure 4: Explaining an image classification prediction made by Google's Inception network, high lighting positive pixels. The top 3 classes predicted are "Electric Guitar" (p = 0.32), "Acoustic guitar" (p = 0.32) and "Laborador" (p = 0.21) Teso, Kersting AIES 2019

AAAI / ACM conference on

**ARTIFICIAL INTELLIGENCE.** 

ETHICS. AND SOCIETY

### The third wave of AI

- Al is more than deep neural networks. Probabilistic and causal models are whiteboxes that provide insights into applications
- Al is more than a single table. Loops, graphs, different data types, relational DBs, ... are central to data science, and highlevel programming languages for DS help to capture this complexity
- Al is more than just Machine Learners and Statisticians

Healthcare calls for AI systems that can acquire human-like communication and reasoning capabilities, with the ability to recognise new situations and adapt to them